NASA TN D-7137

# MODELING OF AIRPLANE PERFORMANCE FROM FLIGHT-TEST RESULTS AND VALIDATION WITH AN F-104G AIRPLANE

by Robert T. Marshall and William G. Schweikhard Flight Research Center Edwards, Calif. 93523

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION • WASHINGTON, D. C. • FEBRUARY 1973

1. Report No. NASA TN D-7137	2. Government Accessi	sion No. 3. Recipient's Catalog No.				
4. Title and Subtitle			5. Report Date			
MODELING OF AIRPLANE PERFO	RMANCE FROM FI	IGHT-TEST	February 197	3		
RESULTS AND VALIDATION WITH		. —	6. Performing Organiza	tion Code		
7. Author(s)			8. Performing Organiza	tion Report No.		
Robert T. Marshall and William G.	Schweikhard	1	H -723			
9. Performing Organization Name and Address		···				
			136-13-08-00-24			
NASA Flight Research Center		1	1. Contract or Grant I	No.		
P. O. Box 273 Edwards, California 93523						
nawaras, camorna coore		1	3. Type of Report and	Period Covered		
12. Sponsoring Agency Name and Address			Technical	Note		
National Aeronautics and Space Adr	ninistration	<u> </u>	4. Sponsoring Agency			
Washington, D. C. 20546			, openioning rigerie,			
15 Complementary Note:						
15. Supplementary Notes						
16. Abstract						
10. Abstract						
		_				
		accurate performance				
		st data and predicted a eristics is developed.				
modeling te	chnique, flight-test	data from level accel	erations are			
used to defi	ne a 1g performanc	e model for the entire	flight envelope			
of an F-104	Gairplane. The pe	erformance model is d rplane and can be vari	lefined in terms			
in ambient	t and drag of the ar	plane weight. The mo	del predicts the			
performance	e of the airplane w	thin 5 percent of the r	neasured flight-			
		ique could substantiall				
		e flight testing and pro g characteristics of a				
definition o	the thrust and dra	g characteristics of a	i aii piane.	•		
· ·						
17. Key Words (Suggested by Author(s))		18. Distribution Statement				
A	ianoa					
Aircraft performance testing techn Performance modeling	iques	_	- 1 1			
Thrust-drag evaluation		Ţ	Inclassified			
	·			<b>-</b> - *		
19. Security Classif. (of this report)	20. Security Classif. (d	of this page)	21. No. of Pages	22. Price*		
Unclassified	Unclassified		28	\$3.00		

# MODELING OF AIRPLANE PERFORMANCE FROM FLIGHT-TEST RESULTS AND VALIDATION WITH AN F-104G AIRPLANE

Robert T. Marshall and William G. Schweikhard Flight Research Center

#### INTRODUCTION

The number of flight tests required to define the performance of modern aircraft and the associated costs of the tests are increasing at an alarming rate. Larger flight envelopes, the multitude of geometric variables (for example, wing sweep or inlet geometry, or both), and the variability of external store configurations of modern high performance aircraft create a matrix of conditions that is nearly impossible to encompass with conventional testing techniques. For this reason, studies are being conducted by NASA to develop a mathematical performance model from flight-test data so that the performance for the entire flight envelope of an aircraft can be determined from a limited number of flight tests.

An aircraft performance model determined from flight-test data can be defined in terms of either excess thrust (thrust minus drag) or the specific values of thrust and drag over the Mach number—altitude operating region. The use of excess thrust data to define an accurate model is limited in that the individual values of thrust and drag are not independently known; therefore, excess thrust must be determined for each geometric configuration and power setting under consideration. Thus many flight tests are necessary to obtain data over the operating envelope of an aircraft. Furthermore, once a model is defined in terms of excess thrust, it is difficult to adjust it to variations from standard-day atmospheric conditions, again because the thrust and drag are combined in one term, making it difficult to separate individual variations of the two parameters. This problem could be eliminated if a performance model were defined in terms of absolute values of thrust and drag. The determination of thrust and drag in flight is a complex, difficult, and tedious process, however, that requires considerably more flight-test time and instrumentation than the definition of excess thrust.

One way to solve this problem would be to develop a technique of defining a performance model for the flight envelope of a particular aircraft configuration from limited flight-test data and the aerodynamic and propulsion system characteristics of the aircraft. Once defined, such a model could be used to predict the flight performance of the aircraft at every point in the flight envelope without additional flight testing. If this could be done, it would reduce the time required for performance flight testing and produce a clear definition of the thrust and drag characteristics of an aircraft. This report presents the results of a study made at the NASA Flight Research Center to develop such a technique. The technique is applied to an F-104G airplane. The measured performance of the airplane is compared with the computed performance of the model.

#### SYMBOLS

Physical quantities in this report are given in the International System of Units (SI)

and parenthetically in U.S. Customary Units. Measurements were taken in Customary Units. Factors relating the two systems are presented in reference 1.

C<sub>D</sub> drag coefficient, D/qS

C<sub>L</sub> lift coefficient, L/qS

D total airplane drag, N (lb)

F net thrust, N (lb)

FU fuel used, kg (lb)

g acceleration due to gravity, 9.8 m/sec<sup>2</sup> (32.2 ft/sec<sup>2</sup>)

g<sub>c</sub> mass-to-force conversion factor, 9.8 N/kg (1 lbf/lbm)

h pressure altitude, m (ft)

he specific energy,  $h + \frac{V^2}{2g}$ , m (ft)

 $\frac{dh}{dt}$  rate of change of altitude, m/sec (ft/sec)

dhe dt rate of change of specific energy, m/sec (ft/sec)

 $K_D$  model coefficient for drag,  $D_l/D_D$ 

 ${
m K_F}$  model coefficient for thrust and fuel flow,  ${
m F_t/F_{p_t}}$  and  ${
m W_{f_t/W_{f_p}}}$ 

L airplane lift, N (lb)

M Mach number

N normal load factor, L/g<sub>c</sub>W

 $p_{t_2}$  compressor inlet total pressure, N/m<sup>2</sup> (lb/in<sup>2</sup>)

q dynamic pressure, N/m<sup>2</sup> (lb/ft<sup>2</sup>)

S wing reference area, m<sup>2</sup> (ft<sup>2</sup>)

SFC specific fuel consumption,  $\frac{\text{kg/sec}}{\text{N}}$  ( $\frac{\text{lb/sec}}{\text{lb}}$ )

T total temperature, °K (°R)

T<sub>a</sub> ambient temperature at altitude, °K (°R)

2

t elapsed time, sec

V velocity along flight path, m/sec (ft/sec)

 $\frac{dV}{dt}$  rate of change of velocity, m/sec<sup>2</sup> (ft/sec<sup>2</sup>)

W airplane gross weight, kg (lb)

W<sub>f</sub> total fuel flow, kg/sec (lb/sec)

 $\alpha$  angle of attack, deg

 $\gamma$  flight path angle, deg

 $\Delta$ ( ) change in specific parameter

 $^{\delta}t_{2}$  compressor inlet total pressure ratio,  $\frac{p_{t_{2}}}{101.33 \times 10^{3}}$ ,  $(\frac{p_{t_{2}}}{14.7})$ 

λ thrust deflection angle, deg

Subscripts:

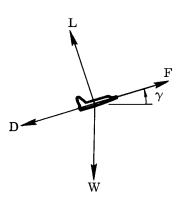
p predicted

s standard day

t test day

## PRINCIPLES OF PERFORMANCE MODELING TECHNIQUES

The term "performance model" is used in its simplest form in this report to refer to a mathematical description of the motion of an aircraft in the vertical plane as given by equations (1) and (2). For this discussion the forces were resolved parallel and perpendicular to the flight path, as indicated in the adjacent sketch, and the angle of attack was assumed to be small.



$$F - D - g_c W \sin \gamma = \frac{g_c W dV}{g dt}$$
 (1)

$$L - g_c W \cos \gamma = g_c W (N - \cos \gamma)$$
 (2)

In the development of the performance model, only nonmaneuvering flight (that is, a normal load factor of 1, constant direction of flight, and constant power setting) was considered. For a normal load factor near 1, equation (2) becomes a secondary correction to the model. As shown in references 2 to 4, equation (1) can be rewritten in terms of the rate of climb, acceleration, and velocity of the airplane as follows:

$$\frac{\left(\mathbf{F}_{t} - \mathbf{D}_{t}\right)\mathbf{V}_{t}}{\mathbf{g}_{c}\mathbf{W}_{t}} = \left(\frac{\mathbf{dh}}{\mathbf{dt}} + \frac{\mathbf{V}\mathbf{dV}}{\mathbf{g}\mathbf{dt}}\right)_{t} \tag{3}$$

The right side of this equation can be determined easily by measuring the velocity and the rates of change of altitude and velocity of an airplane. On the left side of this equation, the weight can also be obtained easily; however, thrust and drag cannot be explicitly defined in flight and are unknowns in the equation. Therefore, a second equation must be developed which allows either the simultaneous solution of the two equations or the determination of an explicit value of thrust or drag.

Experience with in-flight thrust measurements on the XB-70 airplane showed that even though the measured thrust did not usually agree with the predicted thrust, the predicted specific fuel consumption,  $SFC_{D}$ , which is the ratio of fuel flow to thrust, was

generally accurate. The ratio of the measured to the predicted specific fuel consumption is presented in figure 1 for the XB-70 airplane at maximum power. As indicated by the dispersion in the data at any given Mach number, the predicted specific fuel consumption is generally within 5 percent of the measured value. On the basis of this observation, it was assumed that the ratio of the in-flight measured fuel flow to thrust should be approximately equal to the ratio of the predicted fuel flow to thrust corrected for the test-day temperature as shown by equations (4) and (5):

$$SFC_{p_t} = W_{f_{p_t}} / F_{p_t} = W_{f_t} / F_t$$
 (4)

where

The values of  $\Delta W_f$  and  $\Delta F$  are obtained from equations (A5) and (A6) of appendix A. Furthermore, reference 5 indicates that the climb and acceleration performance of an aircraft is fairly insensitive to nominal errors in specific fuel consumption. In reference 5 a  $\pm 10$  percent deviation in specific fuel consumption resulted in a -0.4 to 0.7 percent change in the climb and acceleration performance of an F-111B airplane at maximum power.

A second assumption that must be made for equation (4) to be valid is that the predicted propulsion system characteristics available for the airplane are consistent within themselves. It is also assumed that the relationship of the thrust and fuel flow is accurately described and that the temperature corrections for these quantities are accurate.

If these assumptions are valid, the in-flight thrust can be calculated with equation (4) by measuring the fuel flow and making use of the predicted propulsion system characteristics of the airplane as follows:

$$F_{t} = \left(W_{f_{t}}/W_{f_{p_{t}}}\right)F_{p_{t}}$$
(6)

The drag can then be determined from equation (3). With this technique the thrust and drag of the airplane can be determined for each test point for use in the performance model.

Rather than calculate the thrust and drag for each test point, it was easier to use a model which incorporated the predicted drag, thrust, and fuel flow and then to refine these values by determining a set of coefficients,  $K_F$  and  $K_D$ , so that the performance of the model matched the test-day performance of the airplane. This was done by first computing the coefficient  $K_F$  as defined by equation (6) as follows:

$$K_F = W_{f_t}/W_{f_{p_t}} = F_t/F_{p_t}$$
 (7)

The coefficient  $K_D$  was then determined (for test conditions) from the following version of equation (3):

$$\left[ \frac{\left( \frac{K_F F_{p_t} - K_D D_p}{V} \right)}{g_c W} \right]_{\text{model}} = \left( \frac{dh}{dt} + \frac{V dV}{g dt} \right)_{\text{airplane}}$$
(8)

where

$$K_{D} = D_{t}/D_{p} \tag{9}$$

Values of  $K_F$  and  $K_D$  were determined in this manner for each point in a test trajectory, and since values of predicted thrust and drag were available in the model, the true thrust and drag of the airplane were readily calculated.

The data analysis procedures used in this investigation are discussed in detail in the appendix.

### VALIDATION OF THE PERFORMANCE MODELING TECHNIQUE

The performance modeling technique was validated on the basis of the following criterion: That having determined a set of coefficients ( $K_F$  and  $K_D$ ) from a series of level accelerations performed at different altitudes, weights, and temperatures over the flight envelope of an airplane, it should be possible to calculate the performance of the airplane for any arbitrary flight trajectory encompassing climbs, dives, and accelerations as long as the maneuvering load factor increments are low ( $\pm 0.2g$ ). For the

validation, the modeling technique was applied to level acceleration flight-test data obtained on an instrumented F-104G prototype airplane (fig. 2) and reported in reference 6.

The F-104G is a fixed-wing, fixed-inlet-geometry airplane powered by a J79-GE-11A, high-pressure-ratio, afterburning turbojet engine. The airplane is 16.7 meters (54.8 feet) in length and 4.1 meters (13.5 feet) in height, with a wingspan of 6.7 meters (21.9 feet) and a sea-level ratio of maximum power thrust to weight of 0.78. The test instrumentation, the airplane, and the engine are described in detail in references 6, 7, and 8, respectively.

#### Model Coefficients Computed From Level Acceleration Maneuvers

The model coefficients  $K_F$  and  $K_D$  were determined from the level acceleration flight-test data using a computer program. (See appendix.) The coefficients computed for two level acceleration maneuvers at an altitude of 9144 meters (30,000 feet) are presented in figure 3 together with curves faired through each set of coefficients. The analysis procedure was then repeated for level accelerations made at 3048 meters (10,000 feet), 6096 meters (20,000 feet), 9144 meters (30,000 feet), 12,192 meters (40,000 feet), and 15,240 meters (50,000 feet) to define the model coefficients for each of these test altitudes. The fairings of the coefficients  $K_F$  and  $K_D$  obtained from this analysis are presented in figures 4 and 5, respectively.

A complete performance model of the F-104G test airplane was then obtained by combining the set of model coefficients presented in figures 4 and 5 with the predicted aerodynamic and propulsion system characteristics of the airplane (tables 1 to 4, adapted from refs. 7 and 8) in a digital trajectory analysis computer program. To validate the coefficients, the trajectory program, which constitutes the performance model of the test airplane, was used to compute the model test-day performance for each of the level accelerations, with the test-day Mach number-altitude profile and the test-day temperatures at altitude used as inputs to the program. Computed and measured test-day performance of the airplane for the level accelerations made at 9144 meters (30,000 feet) is compared in figures 6(a) and 6(b). As shown, an excellent match was obtained, thus validating the coefficients for this altitude. The coefficients for the other altitudes were validated in the same manner. The performance model for the test airplane was obtained from approximately 31 minutes of flight-test data.

The computer model could also have been obtained by adjusting the predicted drag polars and the thrust and fuel flow curves in proportion to the model coefficients  $\rm K_F$  and  $\rm K_D$  and then entering these new curves into the program. Although this approach was not used because of the time required to adjust and reprogram the curves each time a coefficient was changed, typical adjusted and predicted drag polars for Mach numbers of 0.90 and 1.60 are presented in figures 7(a) and 7(b).

#### Validation of the Model Using Arbitrary Profiles

To evaluate the validity of the performance model as a whole, model and measured performance for other, arbitrarily chosen flight profiles were compared. The

performance of the test airplane was measured along three different flight profiles flown from a Mach number of approximately 0.90 at an altitude of 3048 meters (10,000 feet) to a Mach number of 2.0 at an altitude of 12,192 meters (40,000 feet). The criterion established to validate the model was that the model and the measured performance of the airplane agree within 5 percent.

The measured performance of the airplane and the computed performance of the model are compared in figures 8(a) to 8(c). The width of the ±5 percent band about the flight data curve indicates the region within which the model data should fall for a satisfactory match. As shown in figure 8(a), a good match of the model and measured performance was obtained for the first flight profile. But for the other two flight profiles (figs. 8(b) and 8(c)), the computed performance does not agree with the measured performance of the airplane within the established 5 percent limit. Approximately 50 percent to 60 percent of the climb in flights B and C was at Mach numbers of 0.95 to 1.0, whereas only 5 percent of the climb in flight A was at these Mach numbers. Thus inaccuracies in the predicted airplane aerodynamics and in the flight-test data in this transonic region, coupled with the length of time spent at these Mach numbers, could have been responsible for the errors encountered at the higher Mach numbers. Consequently, the measured performance of the airplane and the computed performance of he model were compared for the supersonic portions of the flight profiles presented in igures 8(b) and 8(c). The comparisons (figs. 9(a) and 9(b)) show good agreement of the performance data, which verifies the basic assumptions and points out that improved redictions of aerodynamic data, flight-test measurements, and test techniques are needed if the model coefficients in the transonic Mach number region are to be defined nore accurately. Still, the validity of the modeling technique has been demonstrated, and the time and effort required to produce this model has been substantially reduced.

#### Sensitivity of the Coefficients

From the preceding section and equations (6) and (9) it may be inferred that if the model performance exactly matches the measured performance of the test airplane, the in-flight thrust, fuel flow, and drag of the test airplane are defined accurately. Therefore, errors in the values of in-flight thrust, fuel flow, and drag are due to the errors in the final set of coefficients. The errors in the coefficients result from instrumentation, measurement, and data analysis errors in the values of fuel flow, altitude, velocity, rate of change of specific energy, and normal load factor. The sensitivity of the model coefficients to variations in these parameters was determined by increasing each parameter individually by 1 percent and determining the resulting percentage of change in the coefficients. The results of the error determination are presented in figure 10. As shown in figure 10(a), the coefficient  $K_D$  is sensitive to errors in fuel flow, normal load factor, and rate of change of specific energy, especially at Mach numbers less than 1.0. For example, a 1 percent error in fuel flow at Mach 0.75 results in a 4.5 percent change in the value of  $K_D$ . The results are sensitive to altitude at subsonic and supersonic speeds.

Because of the order in which the parameters were used in the modeling analysis, fuel flow was the only parameter which influenced the value of the model coefficient  $K_F$ . The variation in  $K_F$  caused by a 1 percent increase in the fuel flow (fig. 10(b)) shows

that it is sensitive to error in this parameter. Thus the quality of the model coefficients depends on the accuracy with which the flight-test fuel flow, normal load factor, and altitude can be measured and on the accuracy with which the rate of change of specific energy can be calculated.

#### Extension of Modeling Technique

The results of the validation show that a realistic performance model of an airplane can be defined with the modeling technique used in this study and that the assumptions made in the development of the technique were valid. However, to develop a complete performance model of an airplane, the modeling techniques must be extended to cover both partial power and maneuvering flight conditions. Also, the technique was demonstrated only with a fixed-wing, fixed-inlet-geometry airplane. For a complete evaluation it should be extended to airplanes with variable wing sweep, variable inlet geometry, or both. Application of the modeling technique to any airplane is dependent on the ability to account for variations in the aerodynamic and propulsion system parameters resulting from variations in test-day temperatures and aircraft weight.

#### CONCLUDING REMARKS

A technique for defining an airplane performance model in terms of thrust and drag from flight-test data and predicted aerodynamics and propulsion system characteristics of the airplane was developed. With the modeling technique, a nominal 1g performance model was defined for the entire flight envelope of an F-104G airplane from approximately 31 minutes of flight-test data. Use of the technique could substantially reduce the time required for performance flight testing and produce a clear definition of the thrust and drag of an aircraft.

The study showed the sensitivity of the model coefficients to errors in measured and calculated flight-test parameters. The model coefficient for drag was sensitive to errors in fuel flow, normal load factor, altitude, and rate of change of specific energy, and the model coefficient for thrust was sensitive to errors in fuel flow. The accuracy of the performance model defined was therefore dependent on the accuracy with which these flight-test parameters were measured and calculated.

The performance modeling technique was evaluated with flight-test data from the F-104G airplane. The model performance matched the flight-test performance within 5 percent except where large portions of a trajectory were flown at transonic Mach numbers. This lack of agreement pointed out the need for improved flight-test measurements, test techniques, and predicted aerodynamic data if the model coefficients in the transonic Mach number region are to be defined more accurately.

The modeling technique was demonstrated only with a fixed-wing, fixed-inlet-geometry airplane. It should be extended to airplanes with variable wing sweep, variable inlet geometry, or both, for complete evaluation. Also, to develop a complete performance model of an airplane, the modeling technique must be extended to cover partial power and maneuvering flight conditions.

Flight Research Center, National Aeronautics and Space Administration, Edwards, Calif., June 28, 1972.

#### APPENDIX

#### PERFORMANCE MODELING DATA ANALYSIS PROCEDURES

The performance modeling techniques and data analysis procedures used to define a performance model for an F-104G airplane from level acceleration flight-test data are outlined in the following discussion.

The model coefficients  $K_F$  and  $K_D$  were computed from flight-test data, predicted aerodynamic and propulsion system characteristics given in references 7 and 8, and equations (A1 to A12). The flight-test parameters used to compute the coefficients were test-day true velocity,  $V_t$ , pressure altitude,  $h_t$ , Mach number,  $M_t$ , angle of attack,  $\alpha$ , total fuel flow,  $W_{f_t}$ , normal load factor, N, and ambient temperature at altitude,  $T_{a_t}$ .

The instantaneous specific energy (or total energy per pound) of the airplane was computed for each data point as follows:

$$he_t = h_t + \frac{V_t^2}{2g} \tag{A1}$$

The rate of change of the specific energy was then computed by determining the slope at each test point of a smooth curve fitted to a time history of he<sub>t</sub>.

The engine and afterburner fuel-used values for the test airplane were computed for each data point and summed to obtain the instantaneous total fuel used, FU, for the airplane. Instantaneous airplane weight was determined by subtracting the total fuel used at each data point from the airplane weight at engine start. The flight-test fuel flow was then obtained by determining the slope at each data point of a curve fitted to a time history of the total fuel used for each level acceleration with the following equation:

$$W_{f_t} = \frac{d(FU)}{dt}$$
 (A2)

The predicted standard-day values of thrust and fuel flow for the test airplane were obtained from curves given in reference 7 for a maximum afterburner power setting by using the expressions

$$F_p = f(M, h_t) \tag{A3}$$

$$W_{f_p} = f(M, h_t)$$
 (A4)

To compute the predicted test-day values of thrust and fuel flow, the changes in thrust,

 $\Delta F$ , and fuel flow,  $\Delta W_f$ , resulting from nonstandard day temperatures were computed.

Values of  $\Delta F$  and  $\Delta W_f$  were obtained from plots of  $\frac{\Delta F/\delta_{t_2}}{T_s-T_t}$  and  $\frac{\Delta W_f/\delta_{t_2}}{T_s-T_t}$  versus

test-day total temperature, respectively. The data for these plots were obtained from reference 8. The test-day total temperature at altitude was determined from the Mach number and ambient temperature, and the change in thrust and fuel flow was computed as follows:

$$\Delta F = \frac{\frac{\Delta F}{\delta_{t_2}}}{T_s - T_t} (T_s - T_t) \left(\delta_{t_2}\right)$$
(A5)

$$\Delta W_{\mathbf{f}} = \frac{\frac{\Delta W_{\mathbf{f}}}{\delta_{\mathbf{t}_2}}}{T_{\mathbf{s}} - T_{\mathbf{t}}} (T_{\mathbf{s}} - T_{\mathbf{t}}) \left(\delta_{\mathbf{t}_2}\right)$$
(A6)

The model coefficient  $K_{_{\rm F\!P}}$  was calculated for each data point with the expression

$$K_{F} = \frac{W_{f_{t}}}{\left(W_{f_{p_{s}}} + \Delta W_{f}\right)}$$
(A7)

The flight-test thrust of the airplane was then computed by using the expression

$$F_{t} = (F_{p} + \Delta F) K_{F}$$
 (A8)

The total flight-test drag of the airplane was computed as follows:

$$D_{t} = F_{t} - \left[ \left( \frac{dhe}{dt} \right)_{t} \frac{g_{c}W_{t}}{V_{t}} \right]$$
 (A9)

To compute the model coefficient  $K_D$ , the predicted flight-test drag of the airplane was calculated. The predicted drag coefficient was then obtained from the aerodynamic data presented in reference 7 by using the equation

$$C_{D_p} = f(C_{L_t}, M) \tag{A10}$$

where

$$C_{L_{t}} = \frac{1}{qS} \left[ \left( \frac{N}{\cos \alpha} + \frac{(F - D)}{g_{c}W_{t}} \tan \alpha \right) g_{c}W_{t} - F \sin(\alpha - \lambda) \right]$$

The predicted drag of the test airplane for each data point was computed as follows:

$$D_{p} = C_{D_{p}} qS \tag{A11}$$

The model coefficient  $\,\mathrm{K}_{\mathrm{D}}\,$  was computed for each data point using the results of equations (A9) and (A11) and the expression

$$K_{D} = D_{t}/D_{D} \tag{A12}$$

The values of the model coefficients  ${\rm K_F}$  and  ${\rm K_D}$  were plotted against Mach number for each altitude at which a level acceleration maneuver was performed. Then a curve was faired through each set of coefficients. These fairings were combined with the predicted aerodynamic and propulsion system characteristics of the airplane in a two-dimensional trajectory analysis program to define the performance model of the test airplane.

#### REFERENCES

- 1. Mechtly, E. A.: The International System of Units Physical Constants and Conversion Factors. NASA SP-7012, 1969.
- 2. Herrington, Russel M.; Shoemacher, Paul E.; Bartlett, Eugene P.; and Dunlap, Everett W.: Flight Test Engineering Handbook. Tech. Rep. No. 6273, Air Force Flight Test Center, May 1951 (rev. Jan. 1966).
- 3. Godwin, O. D.; Frazier, F. D.; and Durnin, R. E.: Performance Flight Test Techniques. FTC-TIH 64-2006, USAF Aerospace Research Pilot School, Edwards Air Force Base, Calif. [1964].
- 4. Hendrix, George D.; Godwin, Orgle D.; Frazier, Frank D.; and Durnin, Rodney E.: Performance Flight Testing Theory. FTC-TIH 64-2005, USAF Aerospace Research Pilot School, Edwards Air Force Base, Calif. [1964].
- 5. Irons, Robert P., Jr.; Lindquist, O. H.; Schultz, R. L.; et al.: Integrated Engine Instrumentation System Study Energy Management Subsystem Investigation. Volume 1: Basic Document. Rept. No. 12591-FR1 vol. 1, Honeywell, Inc., Apr. 1970. (Available from DDC as AD 872130.)
- 6. Marshall, Robert T.: Flight-Determined Acceleration and Climb Performance of an F-104G Airplane for Use in an Optimum-Flight-Path Computer Program. NASA TN D-6398, 1971.
- 7. Avant, N. J.: Performance Characteristics Appendix A. Rep. No. 16097 App. A, Lockheed Aircraft Corp., July 16, 1962.
- 8. Michaels, J. M.; Wesling, G. C.; Housley, F. R.; and Henderson, R. L.: J79-GE-7, J79-GE-11, J79-GE-11A Turbojet Engine. R60FPD451. Flight Propulsion Div., General Electric, Sept. 1960.

TABLE 1  $\begin{tabular}{ll} VALUES OF LIFT COEFFICIENT FOR THE F-104G AIRPLANE AT SPECIFIC ANGLES \\ OF ATTACK AND MACH NUMBERS \end{tabular}$ 

	C <sub>L</sub> for an M of -										
$lpha, \  ext{deg}$	0.4	0.6	0.8	0.9	1.0	1.2	1.4	1.6	1.8	2.0	
0	0.010	0.010	0.010	0.010	-0.010	-0.020	0,040	0.032	0.020	0.010	
2	.100	.100	.118	.145	.140	. 125	.155	.132	.110	.090	
4	.210	. 215	.270	.300	.300	. 255	. 275	. 235	.200	.175	
6	.318	.330	.415	. 465	.450	.380	.390	.340	.290	. 252	
8	. 430	. 445	.535	.610	.600	.515	.500	. 440	.380	. 330	
10	.540	. 555	.630	.720	.740	.650	.618	.540	.470	.409	
12	.655	.659	.710	.800	.868	.765	.720	.639	.559	.480	
14	.743	.748	.775	.870	.980	.870	.820	.730	.642	.560	

	$^{ m C}_{ m D}$ for a $^{ m C}_{ m L}$ of -										
M	0	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50	
0 .800 .850 .880 .900 .925 .950 .975 1.000 1.050 1.100	0.0160 .0160 .0163 .0170 .0170 .0190 .0230 .0310 .0380 .0470 .0500	0.0175 .0175 .0180 .0184 .0185 .0200 .0240 .0338 .0401 .0485 .0520 .0522	0.0195 .0195 .0197 .0200 .0203 .0219 .0268 .0357 .0420 .0512 .0550	0.0222 .0222 .0220 .0228 .0233 .0250 .0305 .0383 .0455 .0555 .0595	0.0258 .0258 .0260 .0269 .0278 .0295 .0355 .0428 .0509 .0606 .0653	0.0308 .0308 .0315 .0329 .0357 .0417 .0488 .0575 .0670 .0740	0.0378 .0378 .0387 .0402 .0408 .0431 .0488 .0562 .0650 .0763 .0820	0.0462 .0462 .0475 .0491 .0495 .0521 .0578 .0652 .0738 .0870 .0913	0.0562 .0562 .0575 .0591 .0600 .0632 .0685 .0752 .0852 .0990 .1040	0.0673 .0673 .0683 .0700 .0718 .0755 .0802 .0880 .0983 .1118 .1175	
1.200 1.400 1.600 1.800 2.000	.0490 .0468 .0440 .0430 .0422	.0519 .0495 .0470 .0472 .0463	.0553 .0535 .0515 .0523 .0519	.0602 .0589 .0579 .0591 .0590	.0669 .0663 .0663 .0685	.0750 .0758 .0770 .0798 .0815	.0850 .0870 .0895 .0930 .0960	.0959 .1000 .1038 .1085 .1130	.1088 .1145 .1193 .1250 .1315	.1235 .1305 .1360 .1435 .1515	

TABLE 3  $\begin{tabular}{ll} VALUES OF NET THRUST FOR THE F-104G AIRPLANE AT SPECIFIC ALTITUDES AND MACH NUMBERS \end{tabular}$ 

	F, in N (lb), for an M of -										
h, m (ft)	0	0.4	0.6	0.8	1.0	1.2	1.4	1.6	1.8	2.0	
0 (0)	49,820	60,673	66,945	74,596	84, 961	95,859	106, 534	117,210	127, 886	138,561	
	(11,200)	(13,640)	(15,050)	(16,770)	(19, 100)	(21,550)	(23, 950)	(26,350)	(28, <b>7</b> 50)	(31,150)	
3, 048	34,251	44,704	51,154	58,716 $(13,200)$	67, 168	76,509	89, 409	102,309	115,653	128, 998	
(10, 000)	(7,700)	(10,050)	(11,500)		(15, 100)	(17,200)	(20, 100)	(23,000)	(26,000)	(29, 000)	
6,096	20,684	30,559	36,920	43,948	51,822	60,940	71,972	81,180	89,409	97,860	
(20,000)	(4,650)	(6,870)	(8,300)	(9,880)	(11,650)	(13,700)	(16,180)	(18,250)	(20,100)	(22,000)	
9,144	15,124	23,042	26,912	31,137	37,810	45,372	54, 224	62,186	70,415	75,842	
(30,000)	(3,400)	(5,180)	(6,050)	(7,000)	(8,500)	(10,200)	(12, 190)	(13,980)	(15,830)	(17,050)	
12, 192	13,478	16,903	18,593	20,462	23,575	28, 246	34,918	41,947	48,218	54,401	
(40, 000)	(3,030)	(3,800)	(4,180)	(4,600)	(5,300)	(6, 350)	(7,850)	(9,430)	(10,840)	(12,230)	
15,240	7,562	10,008	11,209	12,544	14,457	17,215	21,440	26,111	29, 936	33,273	
(50,000)	(1,700)	(2,250)	(2,520)	(2,820	(3,250)	(3,870)	(4,820)	(5,870)	(6, 730)	(7,480)	
18,288	1,779	4,671	6,183	7,562	9,030	10,809	13,300	16,014	18,682	20,551	
(60,000)	(400)	(1,050)	(1,390)	(1,700)	(2,030)	(2,430)	(2,990)	(3,600)	(4,200)	(4,620)	

 $\begin{tabular}{ll} TABLE~4\\ VALUES~OF~FUEL~FLOW~RATE~FOR~THE~F-104G~AIRPLANE~AT~SPECIFIC\\ ALTITUDES~AND~MACH~NUMBERS\\ \end{tabular}$ 

	Fuel flow rate, in kg/sec (lb/sec), for an M of -										
h, m (ft)	0	0.4	0.6	0.8	1.0	1.2	1.4	1.6	1.8	2.0	
0	3.23	3.97	4.42	5.01	5.86	6.83	7.80	8,77	9.74	10.71	
(0)	(7.13)	(8.75)	(9.75)	(11.05)	(12.91)	(15.05)	(17.19)	(19,33)	(21.47)	(23.61)	
3,048	2.23	2.89	3.27	3.74	4.36	5.14	5.92	6,80	7.68	8.56	
(10,000)	(4.91)	(6.38)	(7.22)	(8.25)	(9.62)	(11.33)	(13.05)	(15,00)	(16.94)	(18.88)	
6,096	1.52	2.05	2.34	2.68	3.13	3.75	4.47	5.30	$6.01 \ (13.25)$	6.71	
(20,000)	(3.36)	(4.52)	(5.16)	(5.91)	(6.91)	(8.27)	(9.86)	(11.69)		(14.80)	
9, 144	1.01	1.43	1.65	1.89	2.21	2.63	3.15	3.73	4.30	4.79	
(30, 000)	(2.22)	(3.16)	(3.63)	(4.16)	(4.88)	(5.80)	(6.94)	(8.22)	(9.47)	(10.55)	
12,192	.50	. 91	1.11	1.32	1.55	1.81	2.15	2.55	2.93	3.20	
(40,000)	(1.11)	(2. 00)	(2.44)	(2.91)	(3.41)	(4.00)	(4.75)	(5.63)	(6.47)	(7.05)	
15,240	. 34	. 63	.77	. 91	1.06	1.22	1.43	1.67	1.90	2. <b>0</b> 5	
(50,000)	(. 75)	(1. 38)	(1.69)	(2. 00)	(2.33)	(2.69)	(3.16)	(3.69)	(4.19)	(4.52)	
18,288	. 04	.30	.43	.55	.68	.80	.94 (2.08)	1.08	1.22	1.31	
(60,000)	(. 08)	(.66)	(.94)	(1.22)	(1.50)	(1.77)		(2.38)	(2.69)	(2.88)	

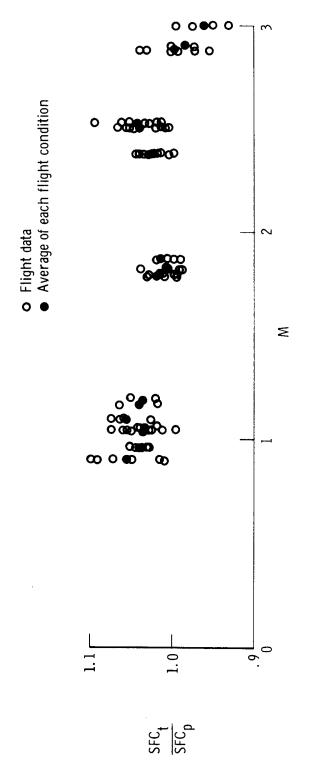


Figure 1. Ratio of measured to predicted specific fuel consumption for the XB-70 airplane at maximum power.

Figure 2. F-104G airplane.

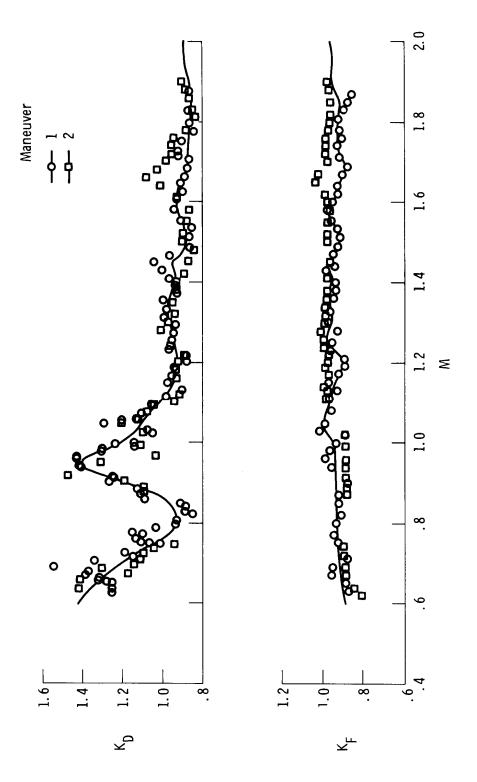


Figure 3. Model coefficients computed from maximum power level accelerations at an altitude of 9144 meters (30,000 feet) for an F-104G airplane.

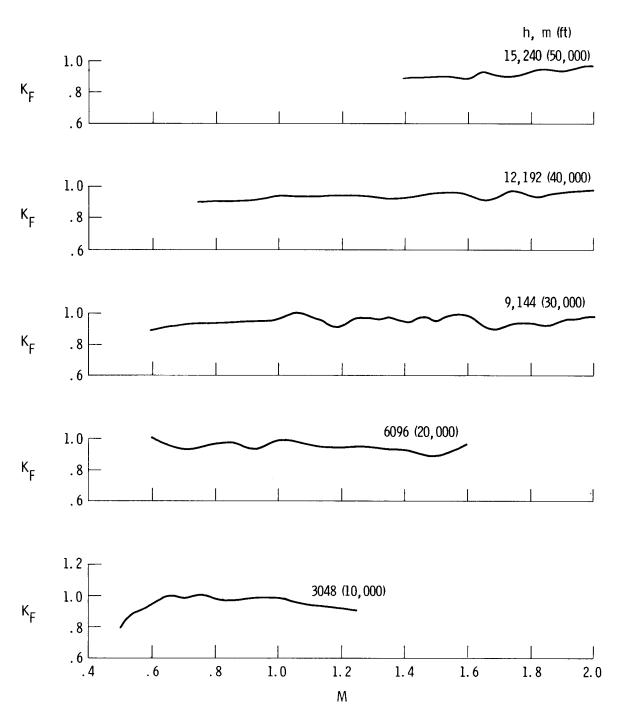


Figure 4. Computed values of model coefficient  $\, {\rm K}_{F} \,$  for thrust and fuel flow for the flight envelope of an F-104G airplane.

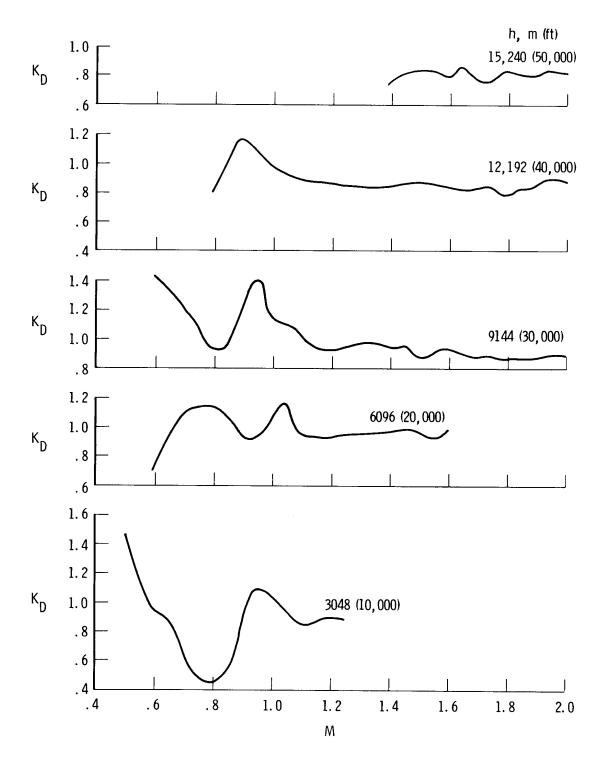


Figure 5. Computed values of model coefficient  $\, {\rm K}_{\rm D} \,$  for drag for the flight envelope of an F-104G airplane.

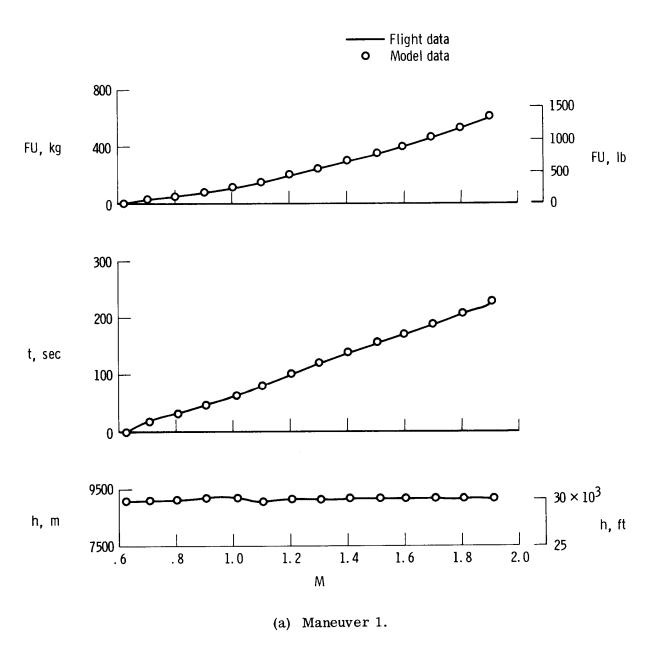


Figure 6. Comparison of flight-test data and model-derived data for a maximum power level acceleration of an F-104G airplane.

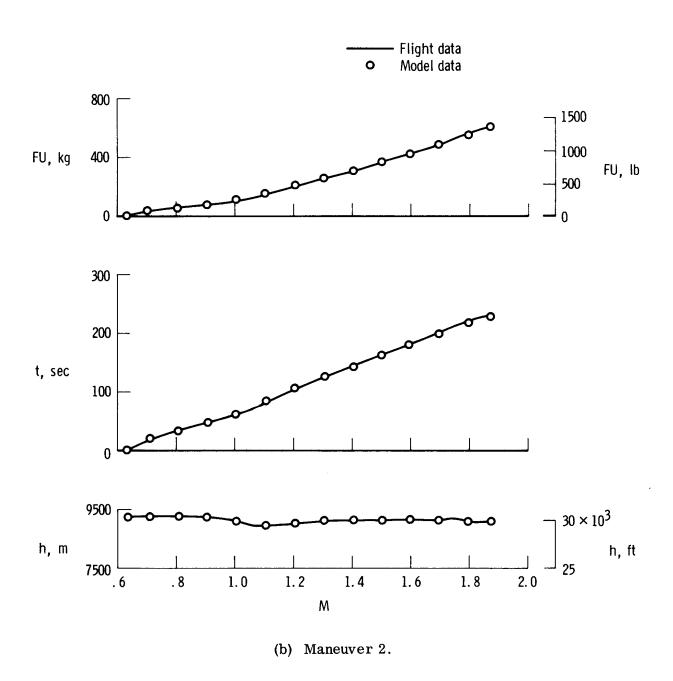


Figure 6. Concluded.

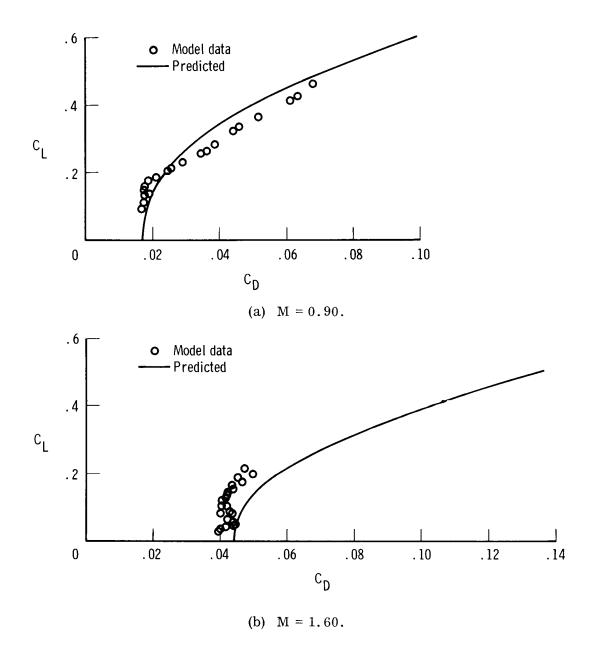


Figure 7. Comparison of adjusted model and predicted drag polars for an F-104G air-plane in a clean configuration.

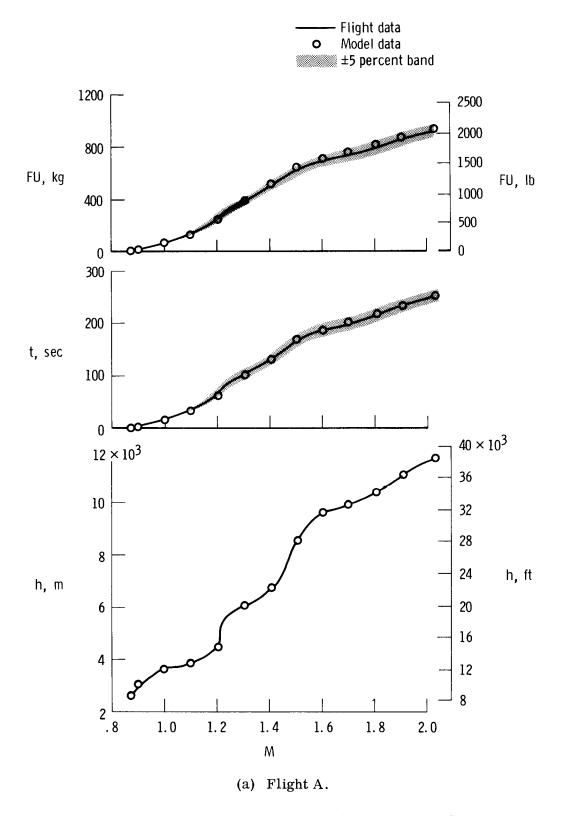


Figure 8. Comparison of flight-test data and model-derived data for maximum power climb of an F-104G airplane.

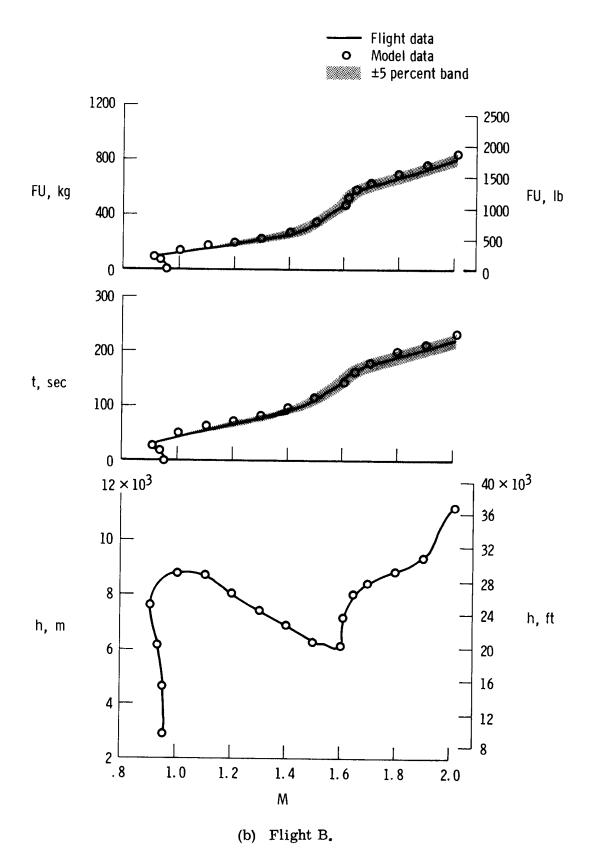


Figure 8. Continued.

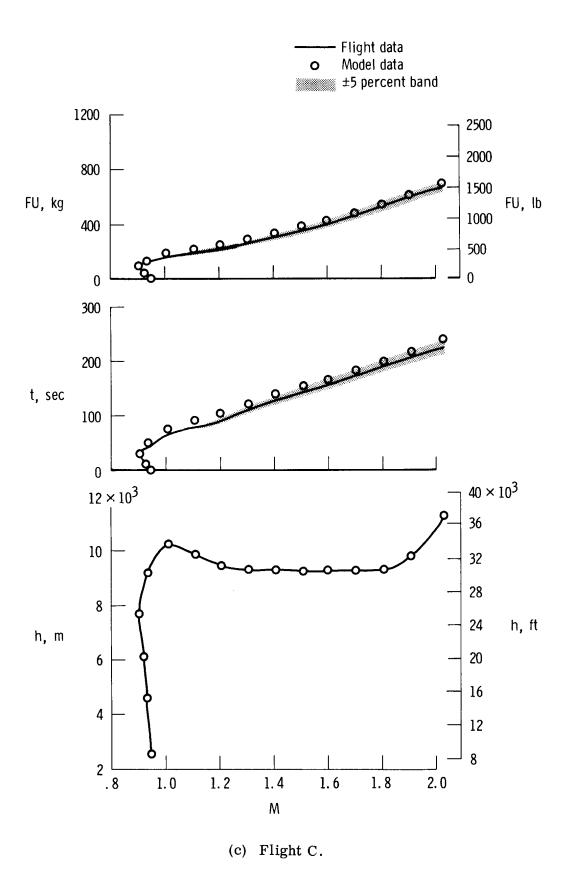


Figure 8. Concluded.

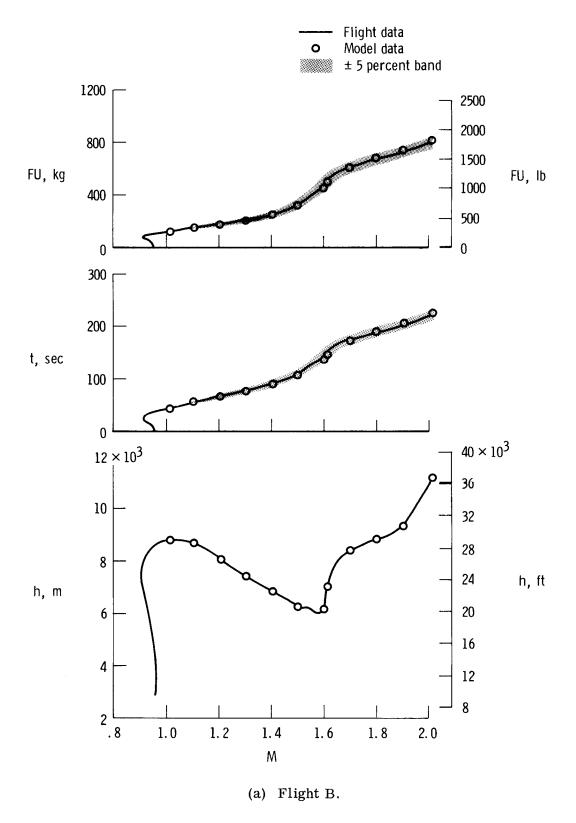


Figure 9. Comparison of flight-test data and model-derived data for the supersonic portion of a flight of an F-104G airplane.

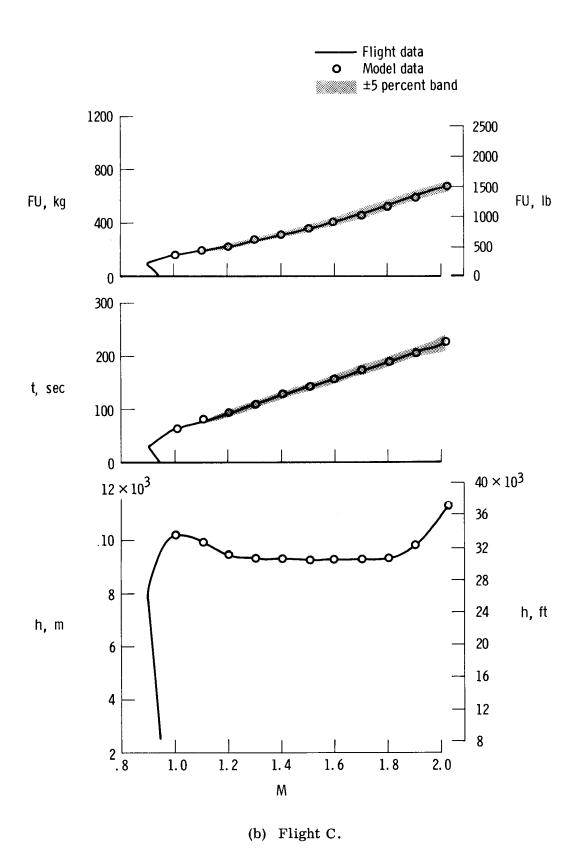


Figure 9. Concluded.

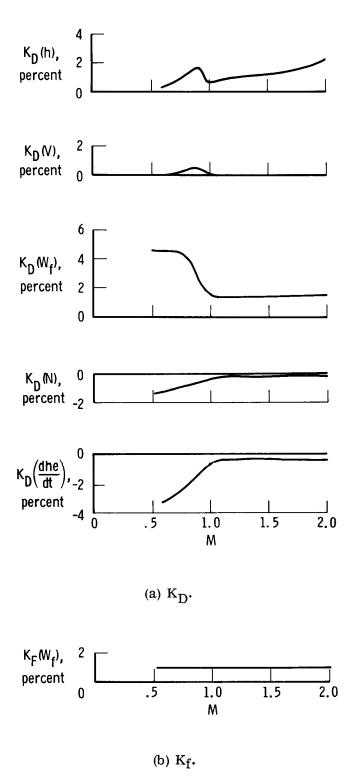


Figure 10. Percentage of change in model coefficients  $\, {\rm K}_{D} \,$  and  $\, {\rm K}_{F} \,$  resulting from a 1 percent increase in important parameters.